

$(a+b)^3$ (+0.1) + 0.1 to Final Exam

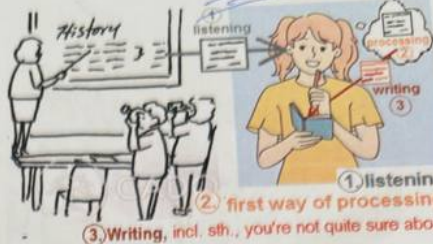
+0.1
for Handout
2025.02.04

+0.1
for A

+0.1
3.5.25



Markoff Chain Probability Model
for Oxford Weather

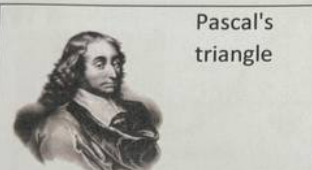


CHALK+TALK **ink+think**
take notes on the lecture yourself

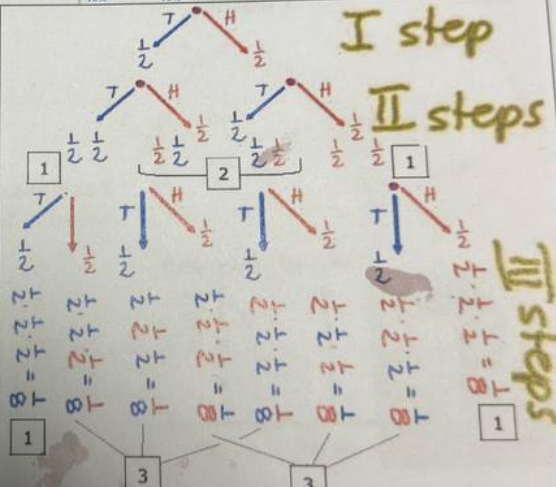
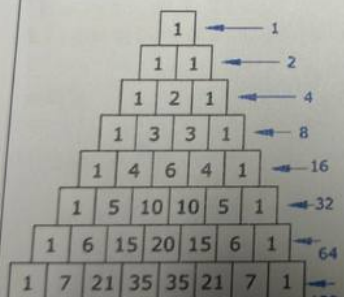
Motivation: 80% chance of rain
Let A_j be the event of rain at Jam on day j of this term, $1 \leq j \leq n$
Suppose the events A_i each have probability p , independently

School = formalism => Uni

Oxford	Tue 13th	Wed 14th	Thu 15th	Fri 16th
	10°	13°	13°	11°
	70%	70%	70%	100%



Pascal's triangle



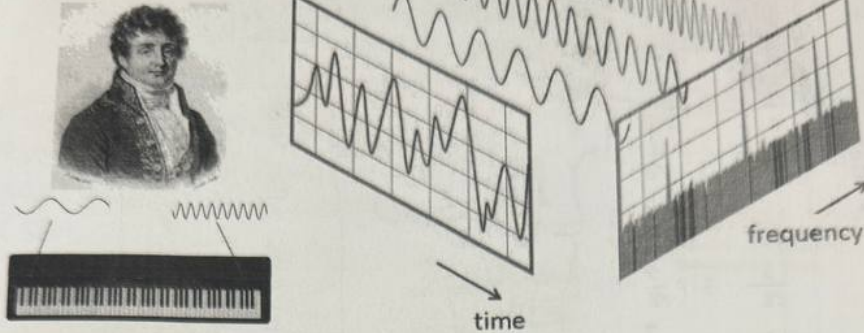
+0.1
to Final

$$\begin{aligned}
 (a+b)^0 &= 1 \\
 (a+b)^1 &= a+b \\
 (a+b)^2 &= a^2 + 2ab + b^2 \\
 (a+b)^3 &= a^3 + 3a^2b + 3ab^2 + b^3 \\
 (a+b)^4 &= a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4 \\
 (a+b)^5 &= a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5 \\
 (a+b)^6 &=
 \end{aligned}$$

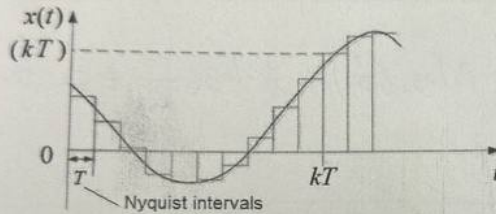
+0.1 to Final Exam Les Misérables

+0.1 to Jim Grade 6.5.25
 +0.1 to Jim Grade

Fourier transform



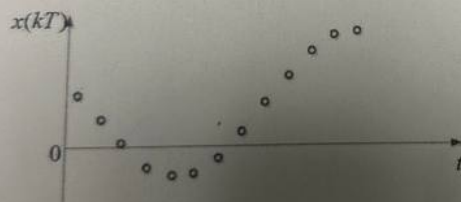
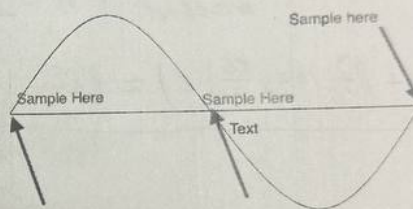
Sampling. Kotelnikov-Nyquist Theorem



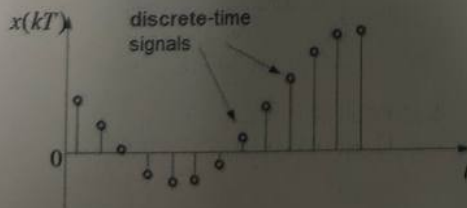
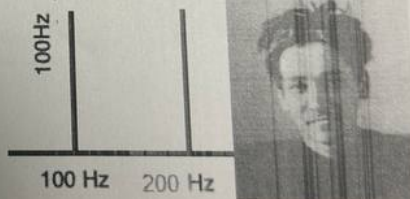
Time intervals T , through which readings $x(kT)$ are taken, are called Nyquist intervals.

Sine with period T

Sampling at $T/2$



frequency Sample



$$F_{\text{sample}} \geq 2 * F_{\text{max}}$$

$$(T_{\text{sample}} \leq T_{\text{min}}/2)$$

Handwritten notes on the left page:

Diagram showing a sequence of symbols: $+++-$ (4 symbols), $+++-$ (4 symbols), $+++-$ (4 symbols), $+++-$ (4 symbols). Total: 16 symbols.

Entropy calculation:

$$H = -\sum p_i \log_2(p_i) = -\frac{6}{16} \log_2 \frac{6}{16} - \frac{4}{16} \log_2 \frac{4}{16} - \frac{3}{16} \log_2 \frac{3}{16} - \frac{3}{16} \log_2 \frac{3}{16}$$

$$= -\frac{6}{16} \log_2 \frac{3}{8} - \frac{4}{16} \log_2 \frac{1}{4} - \frac{3}{16} \log_2 \frac{3}{16} - \frac{3}{16} \log_2 \frac{3}{16}$$

$$= -\frac{6}{16} (\log_2 3 - \log_2 8) - \frac{4}{16} (-2) - \frac{3}{16} (\log_2 3 - \log_2 16) - \frac{3}{16} (\log_2 3 - \log_2 16)$$

$$= -\frac{6}{16} (\log_2 3 - 3) + \frac{4}{16} \cdot 2 - \frac{3}{16} (\log_2 3 - 4) - \frac{3}{16} (\log_2 3 - 4)$$

$$= -\frac{6}{16} \log_2 3 + \frac{18}{16} + \frac{8}{16} - \frac{3}{16} \log_2 3 + \frac{12}{16} - \frac{3}{16} \log_2 3 + \frac{12}{16} - \frac{3}{16} \log_2 3 + \frac{12}{16}$$

$$= -\frac{12}{16} \log_2 3 + \frac{40}{16} = -\frac{3}{4} \log_2 3 + 2.5$$

Approximate value: $2.5 - 0.75 \cdot 1.585 = 2.5 - 1.18875 = 1.31125$

Do tip if I make error

Sir Dr. D. MacKay, University of Cambridge (22 April 1967 - 14 April 2016)

"I believe in clean energy, but I also believe in mathematics"

Diagram illustrating the concept of redundancy in communication:

Transmitted data unit: 1 0 0 1 0 1 1 0

Parity bit: 1

Transmitted data unit: 1 0 0 1 0 1 1 0 1

Diagram showing the flow of information through an encoder, channel, and decoder:

Source: 0 0 0 1 0 1 1 0

Encoder: 0 0 0 1 0 1 1 0 1

Channel: 10%

Decoder: 0 0 0 1 0 1 1 0 1

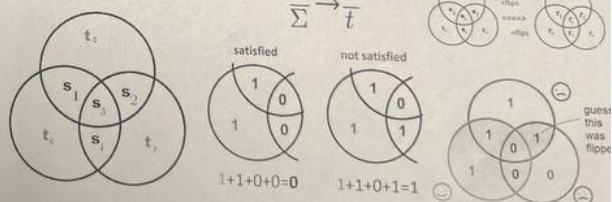
Destination: 0 0 0 1 0 1 1 0

Corrected errors: 0

Undetected errors: 0

7.4. Hamming code.

$$\frac{4}{\Sigma} \rightarrow \frac{7}{t}$$



+0.5 to fun Grade Δ AO@dot.net. By Tanya Ila neepan

Resume of Lecture by Pr. Bob Gallagher from MIT  Massachusetts Institute of Technology (MIT)

George Boole (1815-1864) developed Boolean logic

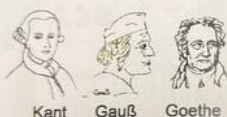
The principles of logical thinking have been understood (and occasionally used) since the Hellenic era.

Boole's contribution was to show how to systemize these principles and express them in equations (called Boolean logic or Boolean algebra).

Claude Shannon (1916-2001) showed how to use Boolean algebra as the basis for switching technology. This contribution systemized logical thinking for computer and communication systems, both for the design and programming of the systems and their applications.

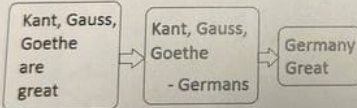
Logic continues to be abused in politics, religion, and most non-scientific areas.

Logic continues to be abused in politics, religion and most non-scientific areas



Kant Gauss Goethe

A little nationalistic, but this is an example of right logic



Bad logic (abuse of logic)

The Mathematical Theory of Communication



Creating a reliable connection over an unreliable (noisy) channel that's what IT is about

and that's what Shannon did

Lecture by Dr. Bob Gallagher
Boole (1815-1864) & Shannon (1916-2001)

Good logic

Sapere aude!
Logical addition (disjunction)

BOOLEAN LOGIC

AND Both terms
OR Either term
NOT Only one term

Socrates was a philosopher
 $S \in \Phi$

philosophers are men
 $\Phi \in A$

Socrates was a man
 $S \in A$

Bad logic

Socrates was a man
 $S \in A$

philosophers are men
 $\Phi \in A$

Socrates was a philosopher
 $S \in \Phi$

noise

message source → encoder → channel → decoder → message receiver

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Pareto Efficiency

Quantity of Gun Produced vs. Quantity of butter Produced

Frontier Pareto
Pareto inefficiency
Pareto efficiency
Impossible point

by Vilfredo Pareto
1848-1903

The orange sector E-D-E is the most Pareto efficient - since an increase in one indicator leads to a decrease in another.

Prisoners' dilemma

Player 1 vs. Player 2

	confess	remain silent
confess	5 years, 5 years	0 year, 20 years
remain silent	20 years, 0 year	1 year, 1 year

Mafia - crime ring

Max protect Penito?

remain silent
confess
0 year
20 years

Game Theory Nash Equilibrium

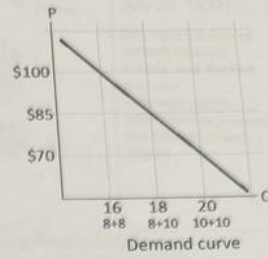
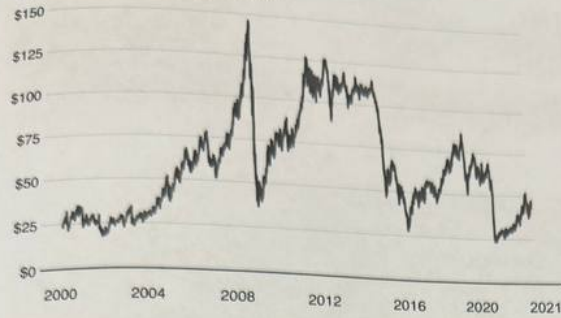
** => Nash equilibrium

	Recognition	Non-recognition
Recognition	1, -5	2, -20
Non-recognition	-20, 0	-1, -1

Pareto Optimality

Oil price hits 18-year low

Brent crude, US dollars per barrel

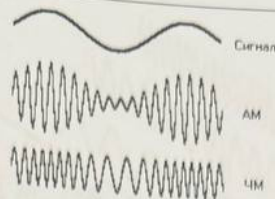


Barrel		1.		2.	
		$8 \cdot 10^6$  day		$10 \cdot 10^6$  day	
1.	$8 \cdot 10^6$ 	 \$800 millions per day <u>\$100</u>   \$800 millions per day	 \$850 millions per day <u>\$85</u>   \$680		
	$10 \cdot 10^6$  day	 \$680 millions per day <u>\$85</u>   \$850 millions per day	 \$700 millions per day <u>\$70</u>   \$700 millions per day		
2.					





Reginald A. Fessenden
(October 6, 1866 – July 22, 1932)

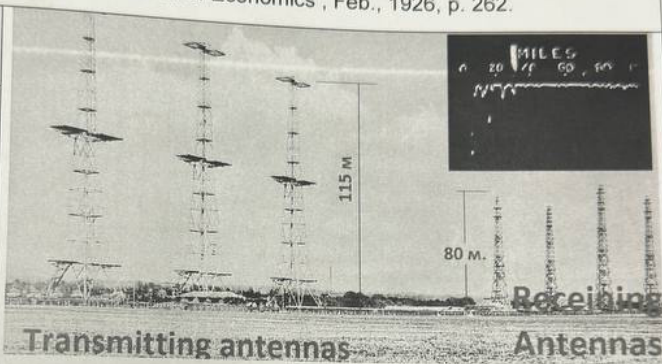
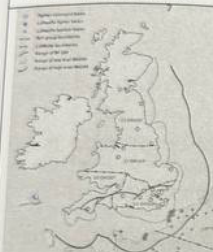


(October 6, 1866 – July 22, 1932)

first transmission of speech by radio (1900), and the first two-way radiotelegraphic communication across the Atlantic Ocean (1906)

"Ни одна организация, занимающаяся какой-либо конкретной областью деятельности, никогда не изобретает какие-либо важные разработки в этой области или не внедряет какие-либо важные разработки в этой области до тех пор, пока она не будет вынуждена сделать это из-за внешней конкуренции.." Oxford University Press. The Quarterly Journal of Economics, Feb., 1926, p. 262.

Battle of Britain
(3 month 3 weeks)
10.07-31.10.1940



Radar played a major role in the Battle of England

H. Nyquist



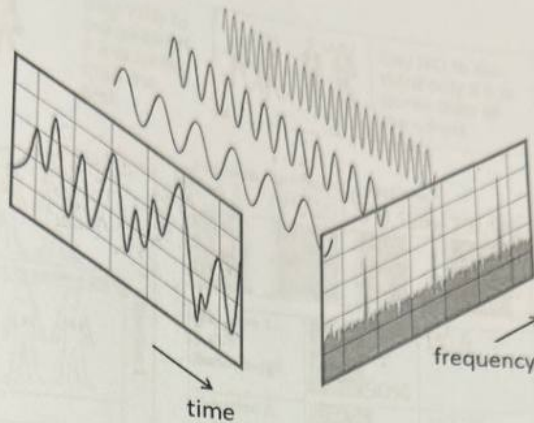
$$W = K \log m$$

Where W is the speed of transmission of intelligence,
 m is the number of current values,
and, K is a constant.

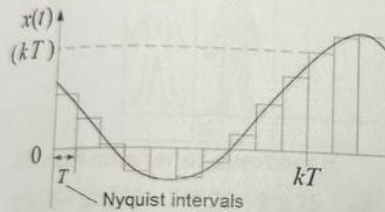


Ralph **Hartley** $H = n \log s$
(81:1888-1970)
 $= \log s^n.$

Fourier transform

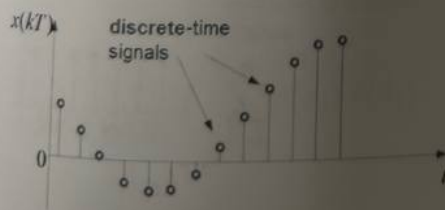
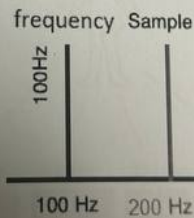
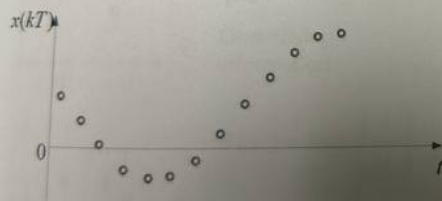
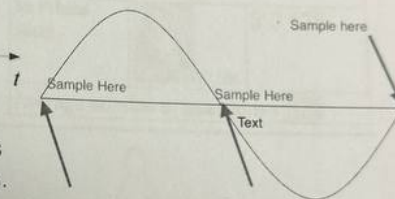


Sampling. Kotelnikov-Nyquist Theorem



Time intervals T , through which readings $s(kT)$ are taken, are called Nyquist intervals.

Sine with period T Sampling at $T/2$



$$F_{\text{sample}} \geq 2 * F_{\text{max}}$$

$$(T_{\text{sample}} \leq T_{\text{min}} / 2)$$



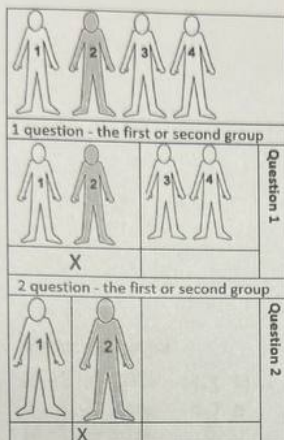
Say NO to the first



Say YES to the second if it is better than the first



Say NO to the third only if it is worse than all the others



Average number of questions =

$$2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 = 2$$

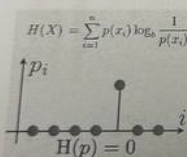
Average number of questions =

$$1 \cdot 0.5 + 2 \cdot 0.25 + 3 \cdot 0.125 + 3 \cdot 0.125$$



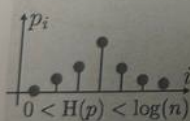
Question 1. Is this Zuckerberg?	 50%	1*0.5
Question 2. Is this Sergey Brin?	 25%	2*0.25
Question 3. Is this Stefan from BMW?	 12.5%	3*0.125
So Prince Saud	 12.5%	3*0.125

Average number of questions = 1.75



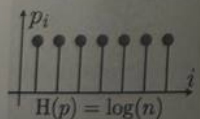
$$\sum_{i=1}^n p(i) \log_2 \frac{1}{p(i)}$$

Quantifying information

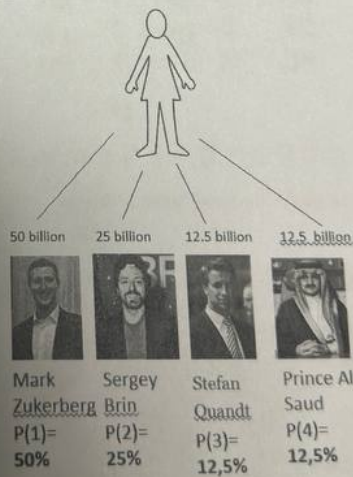


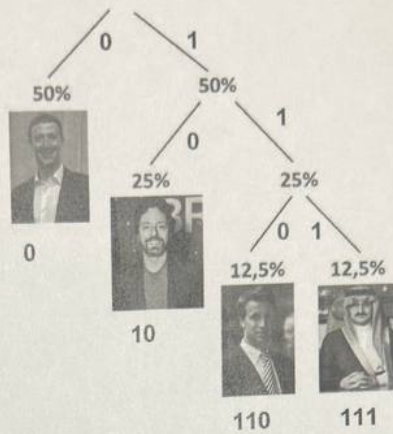
$$I(x_i) = \log_2 \left(\frac{1}{p_i} \right)$$

number of bits required to encode choice



$$\sum_{i=1}^n p(x_i) I(x_i)$$





First-order approximation
(symbols independent but with
frequencies of Belarusian txt)

Мама мыла ра
 М - 3 — 30% 1-3 М
 а - 4 — 40% 4-7 а
 ы - 1 — 10% 8 -ы
 л - 1 — 10% 9 -л
 р - 1 — 10% 10 -р
 10
 лла мама р



Мама мыла ра

Ма - 2 22% 1-2 ма
 ам - 2 22% 3-4 ам
 мы - 1 11% 5 мы
 ыл - 1 11% 6 ыл
 ла - 1 11% 7 ла
 а р - 1 11% 8 ар
 ра - 1 11% 9 ра

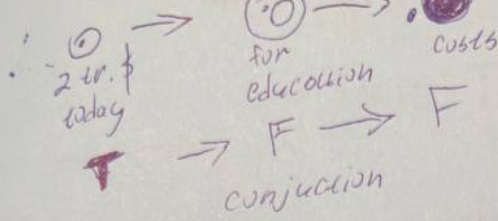
9

0. 4 6 7 3 1 9 1 6 7 3 5
 ам ыл ла ам ма ра ма ыл ла ам мы
 мылла рама



Second-order approximation (digram (2-symbols) structure as in Belarusian)

Logic



Bad logic

+0,2 to fin Exam



Aug mean?

□□□□□ → 5 Blue
 □□ → 2 Red
 □□ → 2 Black
 ■ → 1 Black-Bold

Blue = $\frac{5}{10} = 0.5$ (50%)
 Red = $\frac{2}{10} = 0.2$ (20%)
 Black = $\frac{2}{10} = 0.2$ (20%)
 Black-Bold = $\frac{1}{10} = 0.1$ (10%)

Entropy: $H = -\sum p_i \log_2(p_i)$ or $\sum p_i \log_2(\frac{1}{p_i})$

↓
 $-(0.5 \log_2 0.5 + 0.2 \log_2 0.2 + 0.2 \log_2 0.2 + 0.1 \log_2 0.1) \approx 1.8$ bits

Simple method: $0.5(n-1) = 0.5$ → number of order of a question
 $n=3$
 $0.5 \cdot 2 = 1$
 $0.2 \cdot 2 = 0.4$
 $0.2 \cdot 2 = 0.4$
 $0.1 \cdot 2 = 0.2$
 Sum: 1.8

$0.5 \cdot \log_2(\frac{1}{0.5}) + 0.2 \cdot \log_2(\frac{1}{0.2}) +$
 $0.5 \cdot 1 + 0.2 \cdot 2$

5.5 = 25
 6.6 = 36
 7.7 = 47
 48

$F_n \geq 2 \cdot F_{n-1}$
 $(F_n \leq F_{n+1}/2)$

1
 1 1
 1 2 1
 1 3 3 1
 1 4 6 4 1
 1 5 10 10 5 1
 1 6 15 20 15 6 1
 1 7 21 35 35 21 7 1
 1 8 28 56 70 56 28 8 1

$(a+b)^6 =$
 $a^6 + 6a^5b + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6ab^5 + b^6$
 $(a+b)^7 =$
 $a^7 + 7a^6b + 21a^5b^2 + 35a^4b^3 + 35a^3b^4 + 21a^2b^5 + 7ab^6 + b^7$

$P(A) = \frac{n! \cdot m!}{n!}$ - Binomial Distribution

Arrangements are indistinguishable in objects

AAA BCD 36!

(AAA) (A1A2A3)

Indising. dising.

$\frac{6!}{3!} \Rightarrow$ Number of comb. order = 120

ABBA = $\frac{4!}{2! \cdot 2!} = 6$
 $\frac{4!}{2!} = 12$

$\frac{n!}{m_1! m_2! \dots m_k!} = \frac{n!}{n! \cdot (n-m)!}$ - Final Formula

XOR x
 00 0
 01 1
 10 1
 11 0

& 00 0
 01 0
 10 0
 11 1

and d:
 cd ITP Projects
 class Boole
 ...
 }